

Homework Assignment V

Computer Assignment:

This exercise confirms the feasibility of compressed sensing on real signals, particularly images, where the sparsity level S is unknown and there might be noise in the collected measurements.

The sensing scheme under consideration are: Random Gaussian and Random Subsampling (directly in the pixel domain). You will find the following three images: Phantom (synthetic), Brain (real) and Boat (real). The two sparsifying matrices that you should consider are: DCT and Wavelet (optional). For DCT, you would like to use a small patch size, say 8×8 or 16×16 . However, for Wavelet (optional), you would like to set the patch size to be as large as the image itself. Compute the distortion based on the peak signal-to-noise ratio, often abbreviated PSNR, defined as follows

$$PSNR = 10 \log_{10} \frac{MAX^2}{MSE} \quad \text{where} \quad MSE = \frac{1}{N^2} \|\hat{\mathbf{x}} - \mathbf{x}\|_2^2.$$

For our three test images, $MAX = 255$ (the maximum dynamic range) and N is the image dimension. Use the `psnr.m` file in the package to plot the PSNR between the recovered images and the original with respect to various numbers of measurements M .

What are your observations on how to obtain the best recovery performance? Which sensing scheme is better? Which sensing scheme do you prefer?

Due date: **Thurs, March 8** in lecture